**PROGRAM STRUCTURES AND ALGORITHMS**

**INFO 6205**

**KNAPSACK PROBLEM USING GENETIC ALGORITHM**

**TEAM 508**



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**KNAPSACK PROBLEM**

A knapsack problem or a Rucksack problem is a problem in combinatorial optimization. It states - Given a set of items, each with a weight and a value, determine the number of each item to include in a collection so that the total weight is less than or equal to a given limit and the total value is as large as possible.

For example, consider you are traveling to a different city and you have a limitation on your baggage capacity, and hence there is a limitation on how much and what you can carry. The knapsack algorithm deals with finding a solution to this combinatorial problem.

Let **S** be a set such that S belongs to the items, and let **t** be the target value of the how much weight we can carry. Then, the problem is to find a subset **S’** of S whose elements sum to target t.

One of the problems being solved is the 0/1 Knapsack problem, where the number the xi of copies of each kind of item is restricted to zero or one. Given a set of *n* items numbered from 1 up to *n*, each with a weight wi and a value vi, along with maximum weight capacity W,

Maximize

Subject to

Here, xi represents the number of instances of item *i* to include in the knapsack. Informally, the problem is to maximize the sum of the values of the items in the knapsack so that the sum of the weights is less than or equal to the knapsack's capacity.

**PROBLEM STATEMENT**

One example where Knapsack algorithm is used is the preparation for exam paper just a night before exam. Indian students are mastered in applying the Knapsack solution while exam preparation. Let me explain how.

What is our thinking just a night before exams? Get more marks by less study in the remaining number of hours. Right? So, here we are trying to optimize our efforts for getting more marks. Now, we analyze our previous question papers and decide that which chapters have more value and which chapters have less. We also have a sense that how much time it will take to complete the chapter by checking the number of pages of the chapter in the book.

Here we are trying to maximize the marks by selecting the chapters whose questions have a high probability of asking in the exams. And, we must consider the hours required to complete these chapters. Now we check all the combinations of chapters and their values to find the list of chapters that needs to be studied and, add the hours required to study these chapters so the added hours should not exceed the hours we have for the exam.

This approach of solving the problem for exam preparation is analogous to the 0/1 Knapsack algorithm in which the student either skips the whole chapter and studies the whole chapter.

But wait! The story is not over yet. There are some daredevils among us who further want to reduce their efforts for getting more marks. They still ponder over the previous question papers and realize that some parts of the chapter have more value but not the whole chapter. So, they try to fragment chapter into sections and chose only those sections who have high probability of asking in the exams.

Here they find the highly expected questions in the exams and find the time required for them. Now, they find the ratio of marks for the question and the time required for it.

* *marksForQuestiontime/RequiredForQuestion*

They arrange the ratios into their descending order. Now they select the first question in the order because they know that it is highly expected, and it gives them more marks and it requires less time. And they prepare for the questions one by one in the given order until the hours they have until the exam are completely utilized.

This approach is much more efficient in time and efforts. It is again analogous to the Greedy Knapsack algorithm

in which student breaks the chapters into sections to maximize the marks in the given number of hours.

**In this project, we are aiming to optimize the 0/1 Knapsack problem by implementing it using Genetic Algorithm.**

**GENETIC ALGORITHM**

The genetic algorithm is a method for solving both constrained and unconstrained optimization problems that is based on natural selection, the process that drives biological evolution. The genetic algorithm repeatedly modifies a population of individual solutions. At each step, the genetic algorithm selects individuals at random from the current population to be parents and uses them to produce the children for the next generation. Over successive generations, the population "evolves" toward an optimal solution. You can apply the genetic algorithm to solve a variety of optimization problems that are not well suited for standard optimization algorithms, including problems in which the objective function is discontinuous, nondifferentiable, stochastic, or highly nonlinear. The genetic algorithm can address problems of mixed integer programming, where some components are restricted to be integer-valued.

The genetic algorithm uses three main types of rules at each step to create the next generation from the current population:

* Selection rules select the individuals, called parents, that contribute to the population at the next generation.
* Crossover rules combine two parents to form children for the next generation.
* Mutation rules apply random changes to individual parents to form children.

**How the Genetic Algorithm is implemented in our approach to optimize the Knapsack problem –**

The basic idea of Genetic Algorithm is that it begins with a set of candidate solutions called **population**, and this population is optimized to evolve towards a better solution. Each candidate solution has a set of properties (chromosomes or genotype) which can be mutated and altered. These solutions are represented as strings of 0s and 1s. This evolution usually starts from a population of randomly generated individuals, and is an [**iterative process**](https://en.wikipedia.org/wiki/Iteration), with the population in each iteration called a *generation or an offspring*. Solutions that are chosen to form a new population – the **offspring or new generation,** is selected based on their “**fitness**”. The new generation of candidate solutions is then used in the next iteration of the [algorithm](https://en.wikipedia.org/wiki/Algorithm). Commonly, the algorithm terminates when either a maximum number of generations has been produced, or a satisfactory fitness level has been reached for the population.

We use this approach to repeatedly get a better combination of items to choose from to fit into our knapsack such that the most important and relevant items are picked to fill the knapsack to its capacity.